Modelling Retrieval Models in Probabilistic Logical Models
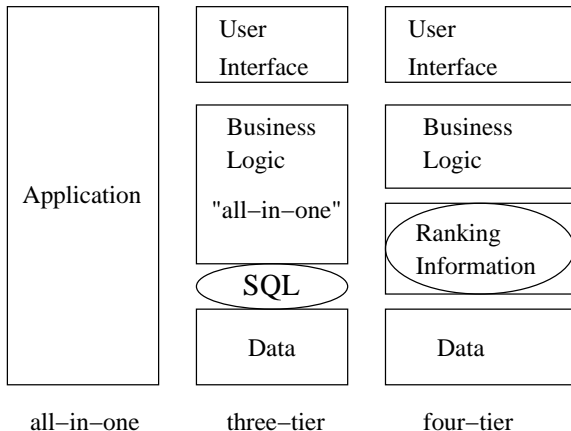
University of Otago, 28th March 2008
Thomas Roelleke
Queen Mary University of London
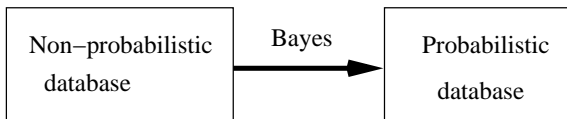
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    - DB+IR Toy Database:
      person(Name, City, Nationality); coll(Term, DocId);
    - Motivation
    - City_Nationality and Nationality_City
    - Syntax and Examples
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Layers

Data and information independence

all–in–one   three–tier   four–tier

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Generation of probabilistic databases

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Layers

External layer	Information sorted by relevance
Logical layer	Probabilistic relations Probability estimation: Bayes[]()
Physical layer	Relational model/algebra; SQL

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Probabilistic Databases
IR-on-DB
(Probabilistic) Retrieval Models
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Example

Probabilistic Databases

[Cavallo and Pittarelli, 1987]: Relational and probabilistic databases, information content (Shannon), probabilistic data dependencies

[Fuhr and Roelleke, 1997]: Probabilistic relational algebra for the integration of IR and DB: intensional vs extensional semantics, event expressions, solve Norbert's "db AND NOT ir OR ir AND NOT db"

[Dalvi and Suciu, 2004]: Efficient query evaluation: intensional semantics and possible worlds semantics, safe-plan optimisation algorithm

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IR-on-DB

[Schek and Pistor, 1982]: Data Structures for an Integrated
Database Management and Information Retrieval
System

[Agrawal et al., 2002, Hristidis and Papakonstantinou, 2002]:
DBXplorer, DISCOVER: keyword search

[Schefe, 1983]: Natuerlichsprachiger Zugang zu Datenbanken?

[Chaudhuri et al., 2004, Chaudhuri et al., 2006]: Probabilistic
ranking of database query results (based on BIR
model)

[Ercegovac et al., 2005]: TEXTURE benchmark (automatic
scaling of benchmark; three competing systems)

[Cornacchia and de Vries, 2007]: A parametrised search
system

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(Probabilistic) Retrieval Models

[Robertson and Sparck Jones, 1976, Croft and Harper, 1979]:
BIR, "the probabilistic model"

[Wong and Yao, 1995, Roelleke et al., 2006]: $P(d \rightarrow q)$ and
matrix framework

[Ponte and Croft, 1998, Hiemstra, 2000, Lafferty and Zhai, 2003]:
language modelling (LM)

[Roelleke, 2003, Robertson, 2004, Robertson, 2005, Roelleke and Wa
"probability of being informative", on theoretical
arguments for idf, on event spaces, a parallel
derivation of probabilistic models

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[Motro, 1988, Motro, 1990, Fuhr, 1990, Bosc and Pivert, 1994]:
vague queries, fuzzy

[Barbara et al., 1992, Lee, 1992, Macleod, 1991]: probabilistic
relational modelling, probability *AGGREGATION*,
text retrieval with SQL

[Niemi and Järvelin, 1995, Fuhr and Roelleke, 1996]: NF2
(non-first-normal-form): [Schek and Scholl, 1986]:
relation-valued attributes

[Robert Ross, 2002]: probabilistic aggregates: the aggregates
underline the difference between "normal"
attributes and tuple probabilities

[Grossman and Frieder, 2004]: implement TF-IDF VSM in SQL

[Roelleke and Fuhr, 1996, Fuhr et al., 1998, Lalmas et al., 2002]
: POOL SIGIR 06, "Dolores" SIGIR 98, POOL (in
Intelligent Exploration of the Web 03), Logic in IR

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Coll	
Term	DocId
sailing	doc1
boats	doc1
sailing	doc2
sailing	doc2
boats	doc2
sailing	doc3
east	doc3
coast	doc3
sailing	doc4
boats	doc5

$\Longrightarrow$

probColl: "tf"		
Prob	Term	DocId
0.5	sailing	doc1
0.5	boats	doc1
0.66	sailing	doc2
0.33	boats	doc2
0.33	sailing	doc3
0.33	east	doc3
0.33	coast	doc3
1.0	sailing	doc4
1.0	boats	doc5

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```
1    −− PSQL
2    INSERT INTO probQuery VALUES
3      0.4 (' sailing ', 'q2'),
4      0.6 ('boats', 'q2');

6    −− Query
7    CREATE VIEW retrieved AS
8      SELECT DocId
9      FROM probQuery, probColl
10     WHERE probQuery.Term = probColl.Term;
```

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non-distinct	
Prob	DocId
$0.4 \cdot 0.5$	doc1
$0.6 \cdot 0.5$	doc1
$0.4 \cdot 0.66$	doc2
$0.6 \cdot 0.33$	doc2
$0.4 \cdot 0.33$	doc3
$0.4 \cdot 1.0$	doc4
$0.6 \cdot 1.0$	doc5

distinct (aggregated)	
Prob	DocId
1.0	doc1
1.0	doc2
$0.4 \cdot 0.33$	doc3
0.4	doc4
0.6	doc5

Aggregation of non-distinct tuples:

```
1   SELECT DISJOINT DocId FROM retrieved;
```

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- Where do the probabilities in probColl ("tf") and probQuery come from?
- How can the estimation be described algebraically?

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person		
Name	City	Nationality
Peter	London	German
Paul	London	Irish
Mary	London	Irish
Thomas	Dortmund	German
Thomas	London	German
Thomas	Hamburg	German
Hany	London	Egyptian
Hany	London	Polish
Jun	London	Chinese
Zhi	London	Chinese

coll	
Term	DocId
sailing	doc1
boats	doc1
sailing	doc2
sailing	doc2
boats	doc2
sailing	doc3
east	doc3
coast	doc3
sailing	doc4
boats	doc5

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City_Nationality		
Prob	City	Nationality
0.500000	"London"	"German"
1.000000	"London"	"Irish"
0.250000	"Dortmund"	"German"
0.250000	"Hamburg"	"German"
1.000000	"London"	"Egyptian"
1.000000	"London"	"Polish"
1.000000	"London"	"Chinese"

```
1  CREATE VIEW City_Nationality AS
2    SELECT DISJOINT City, Nationality
3    FROM person | DISJOINT(Nationality);
```

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Nationality_City		
0.250000	"London"	"German"
0.250000	"London"	"Irish"
1.000000	"Dortmund"	"German"
1.000000	"Hamburg"	"German"
0.125000	"London"	"Egyptian"
0.125000	"London"	"Polish"
0.250000	"London"	"Chinese"

```
1  −− PSQL
2  CREATE VIEW Nationality_City AS
3    SELECT DISJOINT City, Nationality
4    FROM person | DISJOINT(City);
```

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```
# PRA                    -- PSQL
Bayes <estAssumption>    SELECT ... FROM ... WHERE
 [<evidenceKey>](<prae>)  ASSUMPTION <estAssumption>
                          EVIDENCE KEY <evidenceKey>
```

$$\text{evidence} = \text{Project estAssumption}[i1..in](a)$$
$$T := T_a$$
$$P(\tau) = \begin{cases} \frac{P_a(\tau)}{P_{\text{evidence}}(\tau[i_1..i_n])} \\ \frac{\log P_a(\tau)}{\log P_{\text{evidence}}(\tau[i_1..i_n])} \end{cases}$$

In 2003 (early Bayes), Bayes result was distinct; in 2004,
revision led to $T := T_a$.

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Motivation: "Seamlessly" integrated DB+IR technology

- Support document/context and tuple retrieval
- Support free-text and semantic/data retrieval
- Support the flexible modelling of *ALL* retrieval models
- Support the high-level (abstract) modelling of general and specific retrieval tasks (ad-hoc retrieval, classification, summarisation, structured document retrieval, hypertext retrieval, multimedia retrieval, ...)
- Support text, XML, and SQL

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Retrieval Models: RSV's
Retrieval Models: Relationships, Rewritings
Modelling TF-IDF
Modelling BIR
Modelling LM
XML/RDF?

Retrieval Models: Notation Notation ([Roelleke et al., 2006]):

$n_D(t, x)$ number of *Documents* ...

$n_L(t, x)$ number of *Locations* ...

$P_D(t, x) := \frac{n_D(t,x)}{N_D(x)}$ document-based term probability

$P_L(t, x) := \frac{n_L(t,x)}{N_L(x)}$ location-based term probability

...

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Retrieval Models: RSV's

$$RSV_{\text{TF-IDF}}(d, q) := \sum_{t \in q} tf(t, d) \cdot idf(t, c) \tag{1}$$

$$RSV_{\text{BIR}}(d, q) := \sum_{t \in d \cap q} \log \frac{P(t|r)}{P(t|\bar{r})} \tag{2}$$

$$P(q|d) := \prod_{t \in q} [\delta \cdot P(t|d) + (1 - \delta) \cdot P(t|c)] \tag{3}$$

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Retrieval Models: Relationships, Rewritings

$$RSV_{BIR}(d, q) := \sum_{t \in d \cap q} idf(t, \bar{r}) - idf(t, r) \qquad (4)$$

$$RSV_{LM}(d, q) := \log \frac{P(q|d)}{\prod_{t \in q}(1 - \delta) \cdot P(t|c)} \qquad (5)$$

$$= \sum_{t \in q} \log \left[1 + \frac{\delta \cdot P(t|d)}{(1 - \delta) \cdot P(t|c)} \right] \qquad (6)$$

eqn 4: BIR and IDF:
[Robertson, 2004, de Vries and Roelleke, 2005] eqn 6: LM:
[Hiemstra, 2000]
Investigating the relationships important for "good" design of
probabilistic relational modelling.

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```
 1   −− inverse document frequency
 2   CREATE VIEW idf AS
 3       SELECT Term FROM coll
 4       ASSUMPTION MAX INFORMATIVE
 5       EVIDENCE KEY ();

 7   −− query term weighting
 8   CREATE VIEW wQuery AS
 9       SELECT Term, QueryId FROM Query, idf
10       WHERE Query.Term = idf.Term;

12   −− normalisation
13   CREATE VIEW norm_wQuery AS
14       SELECT Term, QueryId FROM wQuery
15       EVIDENCE KEY (QueryId);
```

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```
1   −− retrieve documents
2   CREATE VIEW std_tf_idf_retrieve AS
3       SELECT DISJOINT DocId, QueryId
4       FROM norm_wQuery, tf
5       WHERE norm_wQuery.Term = tf.Term;
```

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```
# tf := P(t|d)                -- P(t occurs | d)
tf =                          CREATE VIEW tf AS
 Project DISJOINT(              SELECT DISJOINT Term, DocId
  Bayes DISJOINT[$2](coll));    FROM coll |
                                       DISJOINT (DocId);
# idf(t,c) :=
# -log P(t|c) /               -- P(t informs | c)
# max_idf(c)                  CREATE VIEW idf AS
idf =                           SELECT Term
 Bayes MAX_IDF[](               FROM coll
  Project[$1](coll));           ASSUMPTION MAX_IDF
                                EVIDENCE KEY ();
```

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```
 1   −− idf in  collection  /  non−relevant:
 2   CREATE VIEW idf_c AS
 3       SELECT Term FROM coll
 4       ASSUMPTION MAX_IDF
 5       EVIDENCE KEY ();

 7   −− idf in  relevant:
 8   CREATE VIEW idf_r AS
 9       SELECT Term FROM relColl
10       ASSUMPTION MAX_IDF
11       EVIDENCE KEY ();
```

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```
1   CREATE VIEW docModel AS
2       SELECT Term, DocId FROM lambda1, p_t_d;

4   CREATE VIEW collModel AS
5       SELECT Term, DocId FROM lambda2, p_t_c, retrieved;

7   -- combine document and collection models
8   CREATE VIEW lm1_mix AS
9       docModel UNION DISJOINT collModel;

11  -- retrieve documents
12  CREATE VIEW lm1_retrieve AS
13      SELECT SUM_LOG DocId, QueryId
14      FROM Query, lm1_mix
15      WHERE Query.Term = lm1_mix.Term;
```

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- accessibility dimension [Roelleke et al., 2002]: tf-idf-acc:

$$tf(t, \text{parent}) := \frac{1}{\sqrt{n}} \cdot tf(t, \text{child})$$

- context-specific informativeness
  [Wang and Roelleke, 2006], IR Theory Glasgow 2006,:
  type- and ancestor-specific idf in retrieval functions

$$RSV(d, q) := \sum_t tf(t, q) \cdot tf(t, d) \cdot idf(t, \text{type}(d), \text{ancestor}(d))$$

- POOL [Roelleke and Fuhr, 1996, Fuhr et al., 1998,
  Lalmas et al., 2002]:
  ```
  ?- D[sailing] & D.author(X) & D1.author(Y) & D1[
  sailor(Y) & Y.friend(X) ]
  ```

Implementation

- Retrieval of $P(t|c)$ probabilities in $O(1)$ (special index)
- Incremental update facility
- $P(t|d)$ probabilities/views are materialised off-line; future research
- Difficulty: System A runs SQL, System B runs PSQL: How to compare?
- top-k and early-response processing

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Summary

- Probabilistic DB, IR-on-DB, PRA, Retrieval Models
- The magnificent five (Select, Project, Join/Multiply, Unite, Subtract): describe probability *AGGREGATION*
- The relational Bayes: describe probability *ESTIMATION*
- DB+IR requires "relaxed" probability theory
    - *idf*-based ("informativeness") probabilities
    - here and there, relax the boundaries of probabilistic modelling and rethink the genuine formulation of IR models
- Scalability: $O(1)$ retrieval of Bayes tuples for $P(t|c)$, given Bayes-oriented indexing structure

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- Database/tuple ranking: modelling and application of retrieval models to SELECT-FROM-WHERE; entropy-based ranking
- Design and verification of probabilistic logical programs
- Optimisation: Semantic, algebraic, and processing (Hengzhi Wu)
- High-level languages: RDF-SPARQL $\rightarrow$ PSQL/PRA (Hany Azzam)
- POLIS: Probabilistic Object-oriented logic for information summarisation (Fred Forst)
- POLAR: Probabilistic Object-oriented annotation-based retrieval (Ingo Frommholz)

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